

Theory on Genetic Diversity Analysis

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A word cloud centered around the word "genetic species". Other prominent words include "genotype", "chromosome", "hybridization", "improvement", "analysis", "diploid", "genes", "seeds", "wild gene", "drought", "different dna", "cultivars", "genet", "use", "genus", "genome", "plant", "crop", "lines", "seed", "crops", "origin", "important", "stress", "resistance", "new variation", "germplasm", "markers", "plants", "accessions", "breeding", "studies", "yield", "cultivated", "molecular", "production", "hybrids", "development". The words are colored in various shades of orange, pink, purple, and blue.

💡 Outline:

Some definitions

Population Genetics
Genetic Markers

Genetic Distances

Intraspecific Diversity

Anova & Complete Randomized Design
Wright Statistics

Find Clusters and Groups

The software BIO-R

Getting BIO-R
Check Output and Estimates

Some Definitions ...

- **Genotype:**

Genotype is ... 

- **Markers:**

Genetic Markers are ... 

- **Population:** ... [CONT]

Population Genetics ...

- **Population Genetics:** Studies the heredity's mechanisms at the population level.
- **Population:** Set of conspecifics individuals in the *same place and time*, which have the ability to mate (exchange alleles).



In a population, the individual has a transitory importance, what matters are the alleles it has, which will be transmitted to subsequent generations

Reproductive systems

- **Allogamous:** frequency of cross pollination is $\geq 95\%$ e.g., maize
- **Autogamous:** frequency of cross pollination is $\leq 5\%$ e.g., wheat.

Allele and Genotypic Frequencies ...

Genotype		Phenotype	Observed	Frequency
BB	→	White	100	0.05
Bb	→	Yellow	1000	0.50
bb	→	Red	900	0.45
Total:			2000	1.00

$$f(B) = p = 0.05 + \frac{0.50}{2} = 0.30$$

$$\begin{aligned} f(b) &= q = 0.45 + \frac{0.50}{2} = 0.70 \\ &= (1 - p) \end{aligned}$$

ONION IS A AUTOGAMOUS SPECIE ...

Any plant can mate with any other one i.e., panmixia & HWE

		<i>B</i>	<i>b</i>
		<i>p</i>	<i>q</i>
<i>B</i>	<i>p</i>	p^2	$p \cdot q$
<i>b</i>	<i>q</i>	$p \cdot q$	q^2

<i>BB</i>	p^2	$0,30^3 = 0,09$
<i>Bb</i>	$2 \cdot p \cdot q$	$2 \cdot 0,30 \cdot 0,70 = 0,42$
<i>bb</i>	q^2	$0,70^2 = 0,49$

IF NOT, CONSIDERING SELFCROSS ...*The plants mate by themselves*

Genotype	G_0	G_1
BB	$p^2 = f_{BB_0}$	$f_{BB_0} + 1/4 \cdot f_{Bb_0}$
Bb	$2 \cdot p \cdot q = f_{Bb_0}$	$f_{Bb_0} - 1/2 \cdot f_{Bb_0}$
bb	$q^2 = f_{bb_0}$	$f_{bb_0} + 1/4 \cdot f_{Bb_0}$

$$\begin{aligned}
 p' &= p^2 + 1/2 \cdot p \cdot q + 1/2 \cdot p \cdot q \\
 &= p^2 + 1/2 \cdot p \cdot (1-p) + 1/2 \cdot p \cdot (1-p) \\
 &= p^2 + 1/2 \cdot (p^2 - p) + 1/2 \cdot (p^2 - p) \\
 &= p^2 + 1/2 \cdot p^2 - 1/2 \cdot p + 1/2 \cdot p^2 - 1/2 \cdot p \\
 &= p^2 - p^2 + p \\
 p' &= p
 \end{aligned}$$

1. Alogamous

$$f_{BB} := p^2$$

$$f_{Bb} := 2 \cdot p \cdot q$$

$$f_{bb} := q^2$$

2. Autogamous

$$f_{BB} := p^2 + 1/2 \cdot p \cdot q$$

$$f_{Bb} := 2 \cdot p \cdot q - 1/2^* \cdot 2 \cdot p \cdot q$$

$$f_{bb} := q^2 + 1/2 \cdot p \cdot q$$

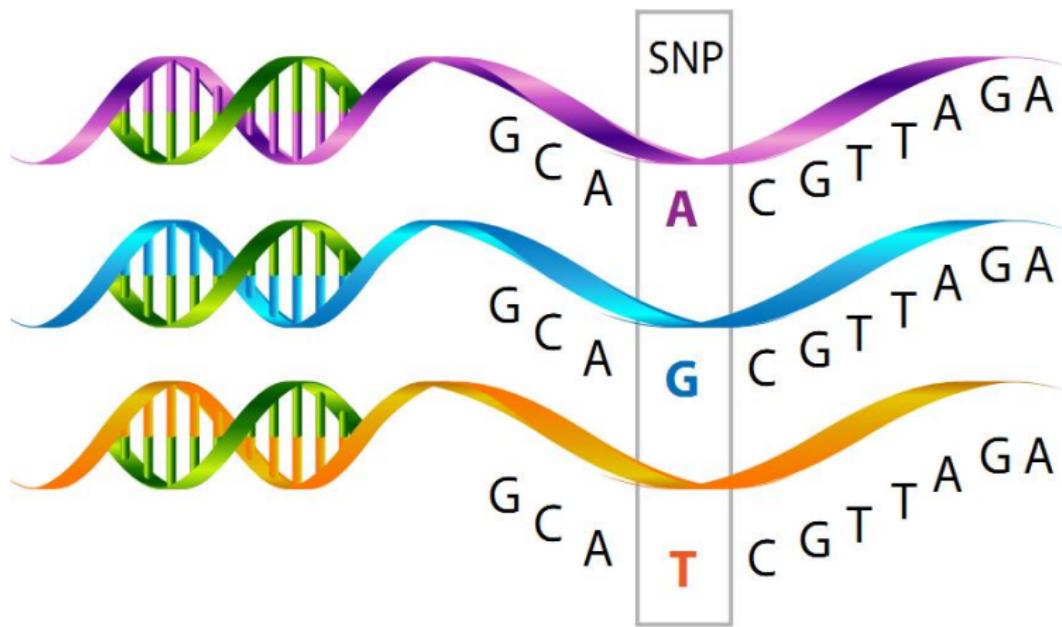
3. Mixed type... taking ${}^*1/2 = I$ or Wright's Equilibrium

$$f_{BB} := p^2 + I \cdot p \cdot q$$

$$f_{Bb} := 2 \cdot p \cdot q - I \cdot 2 \cdot p \cdot q$$

$$f_{bb} := q^2 + I \cdot p \cdot q$$

≠ Genetic Markers ...



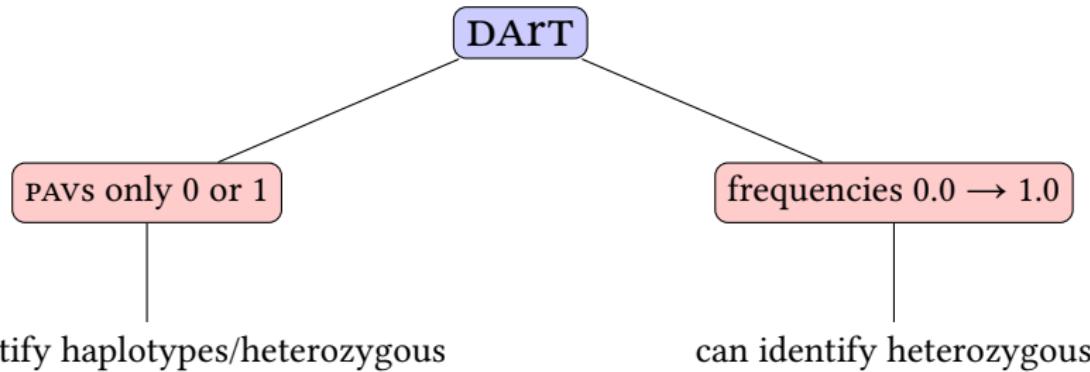
Examples

Marker	Amount	Expression	Polymorphic degree	Specific by locus
Isoenzyme	< 100	codominant	low	✓
RFLP	∞	codominant	medium	✓
RAPD	∞	dominant	medium	–
SSR	∞	codominant	very high	✓
SCAR	∞*	both	low	✓
AFLP	∞	dominant	high	–
SNP	∞	codominant	very high	✓
DART	∞	both	very high	✓**

* After the deployment of other kind of markers.

** Clone aren't but markers are.

DART flexibility...



Maize Bulks w/ frequencies

Marker	Allele	Bulks					
		1	2	3	4	...	g
1	1	0.67	NA*	0.57	NA	...	0.36
1	2	0.33	NA	0.43	NA	...	0.64
2	1	NA	1.00	1.00	1.00	...	1.00
2	2	NA	0.00	0.00	0.00	...	0.00
:	:	:	:	:	:	:	:
m	1	0.00	NA	1.00	0.00	...	1.00
m	2	1.00	NA	0.00	1.00	...	0.00

* NA means Not Available or missing.

Frequencies, so:

$$p + q = 0.67 + 0.33 = 1.00$$

Maize Genotypes w/ *PAV* – (presence/absence)

Marker	Allele	Bulks						
		1	2	3	4	...	g	
1	1	1	NA	1	NA	...	1	
2	1	NA	1	1	1	...	1	
:	:	:	:	:	:	:	:	
<i>m</i>	1	1	NA	1	1	...	1	

* NA means Not Available or missing.

Allele is always 1...the reference allele.



When Genotypes belong to the same bulk, the summary of their *PAV* generates frequencies

≠ Genetic Distances ...

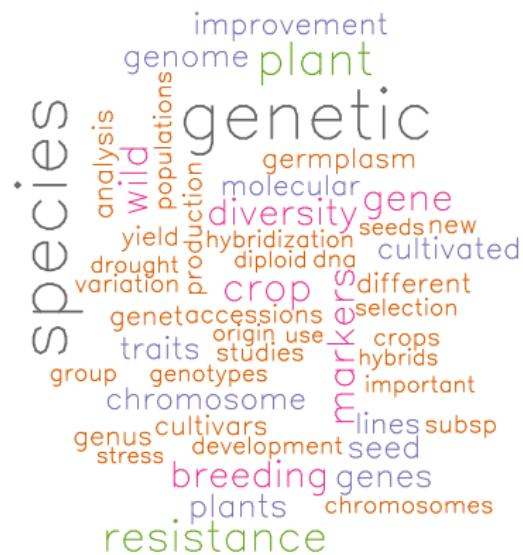
Genetic Distances

Markers w/ allelic information

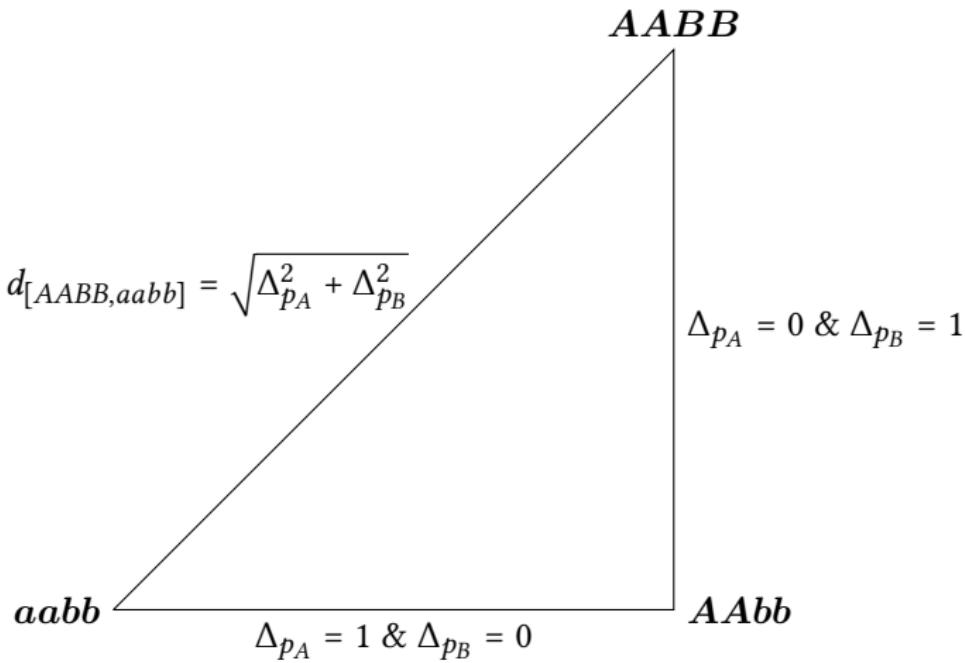
For example: SSR, SNP and DART.

- Euclidean;
- Modified Rogers; and
- Cavalli-Sforza & Edwards.

References: [1, 2, 3]



Euclidean Distance ...



So, ...:

$$Ed_{[x,y]} = \sqrt{\sum_l^L \sum_a^A (\hat{p}_{xla} - \hat{p}_{yla})^2}, \quad (0.0 \leq Ed_{[x,y]} \leq \sqrt{2L^*})$$

where:

\hat{p}_{xla} is the allele frequency for allele a at *locus l* in the genotypes x ;

\hat{p}_{yla} is the same as above for genotype y ;

L is the number of *locus*; and

A is the number of alleles at *locus l*.

*This is the estimator and its respective domain as shown by [3].

≠ Roger's Distance ...

$$Rd_{[x,y]} = \frac{1}{L} \sum_l^L \sqrt{\frac{1}{2} \sum_a^A (\hat{p}_{x la} - \hat{p}_{y la})^2}, \quad (0.0 \leq Rd_{[x,y]} \leq 1.0)$$

where:

$\hat{p}_{x la}$ is the allele frequency for allele a at *locus l* in the genotypes x ;

$\hat{p}_{y la}$ is the same as above for genotype y ;

L is the number of *locus*; and

A is the number of alleles at *locus l*.

It hasn't relationship with Euclidean Geometry. So, ...

Modified Roger's Distance ...

$$MRd_{[x,y]} = \frac{1}{\sqrt{2L}} \sqrt{\sum_l^L \sum_a^A (\hat{p}_{xla} - \hat{p}_{yla})^2}, \quad (0.0 \leq MRd_{[x,y]} \leq 1.0)$$

where:

\hat{p}_{xla} is the allele frequency for allele a at *locus l* in the genotypes x ;

\hat{p}_{yla} is the same as above for genotype y ;

L is the number of *locus*; and

A is the number of alleles at *locus l*.

For non-diploid species, replace $2L$ by the number of copies.

 Cavalli-Sforza & Edwards ...

$$Cd_{[x,y]} = \sqrt{\frac{1}{L} \sum_l^L \left(1 - \sum_a^A \sqrt{\hat{p}_{xla} \times \hat{p}_{yla}} \right)}, \quad (0.0 \leq Cd_{[x,y]} \leq 1.0)$$

where:

\hat{p}_{xla} is the allele frequency for allele a at *locus l* in the genotypes x ;

\hat{p}_{yla} is the same as above for genotype y ;

L is the number of *locus*; and

A is the number of alleles at *locus l*.

≠ Means, Variances and Standard Errors ...

$d_{[x,y]}$ is the distance between genotypes x and y , thus:

- **Mean:** $\mu_{d_{[x,y]}} = \frac{1}{\frac{A(A-1)}{2}} \sum_{x < y} d_{[x,y]}$;
- **Variance:** $\sigma_{d_{[x,y]}}^2 = \frac{1}{\frac{A(A-1)}{2} - 1} \sum_{x < y} (d_{[x,y]} - \mu_{d_{[x,y]}})^2$; and
- **Standard Error:** $S_{\bar{d}_{[x,y]}} = \sqrt{\frac{\sigma_{d_{[x,y]}}^2}{\frac{A(A-1)}{2}}}$.



$\frac{A(A-1)}{2}$ is the 2×2 combination of the alleles i.e., pairs in the distances estimators

✗ Markers w/o Allelic Information ...

		Genotype x	
		1	0
Genotype y	1	a	b
	0	c	d

- **Simple Matching:** $d_{[x,y]} = \frac{b+c}{a+b+c+d};$
- **Jaccard:** $d_{[x,y]} = \frac{b+c}{a+b+c};$ and
- **Nei and Li (or Dice):** $d_{[x,y]} = \frac{2(b+c)}{2a+b+c}.$

The same references for the previous cases i.e., [1, 2, 3].

≠ Diversity Indices ...



A locus is polymorphic if, and only if, its allele frequency is ≤ 0.95 or 0.99

HOLLYWOOD HEIGHT CHART



≠ Raw ...

- Polymorphic proportion:

$$P = \frac{n_{poly}}{n_{total}}$$

- Mean allele number by locus:

$$n_a = \frac{1}{L} \sum_l^L n_l$$

≠ Applied ...

- Observed Heterozygosity (H_o);
- Expected Heterozygosity (H_e);
- Effective Number of Alleles (Ae); and
- Shannon Index (SH).

Observed Heterozygosity:

It is defined as the percentage of heterozygous loci per individual or the number of heterozygous individuals per locus.

Expected Heterozygosity:

$$He = \frac{1}{L} \sum_l^L \left(1 - \sum_a^A \hat{p}_{la}^2 \right) , (0.0 \leq He \leq 1.0)$$

where:

\hat{p}_{la} is the estimated frequency of the allele a at locus l ; and
the other quantities (L and A) were already defined.



NOTE:

$$\sum_a^A \hat{p}_{la} = 1.0$$

Effective Number of Alleles:

$$Ae_l = \frac{1}{\sum_a^A \hat{p}_a^2}$$
$$Ae = \frac{1}{L} \sum_l Ae_l$$



NOTE:

$$Ae_l = \frac{1}{1 - He_l}$$

Shannon Index:

- Total Frequencies:

$$SH_{\text{Total}} = - \sum_a^A \hat{p}_a \log_{10} (\hat{p}_a) , \sum_a^A \hat{p}_a = 1.0$$

- By Locus Frequencies:

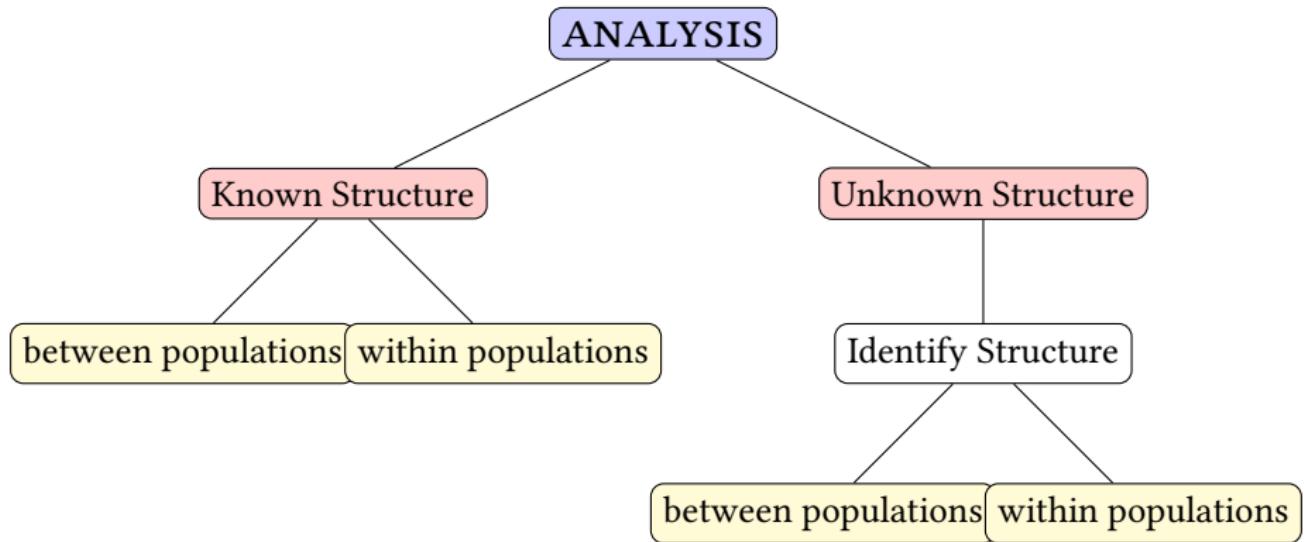
$$SH_{\text{Locus}} = - \sum_a^A \hat{p}_a \log_2 (\hat{p}_a) , \sum_a^A \hat{p}_a = L : (0.0 \leq SH_{\text{Locus}} \leq L)$$

Diversity Indices for PAVs

Statistics:

- Polymorphic proportion _____
- Mean number of alleles by locus _____
- Observed Heterozygosity (H_o) _____
- Expected Heterozygosity (H_e) _____
- Effective Number of Alleles (A_e) _____
- Shannon Index (SH) _____

≠ Intraspecific Diversity ...





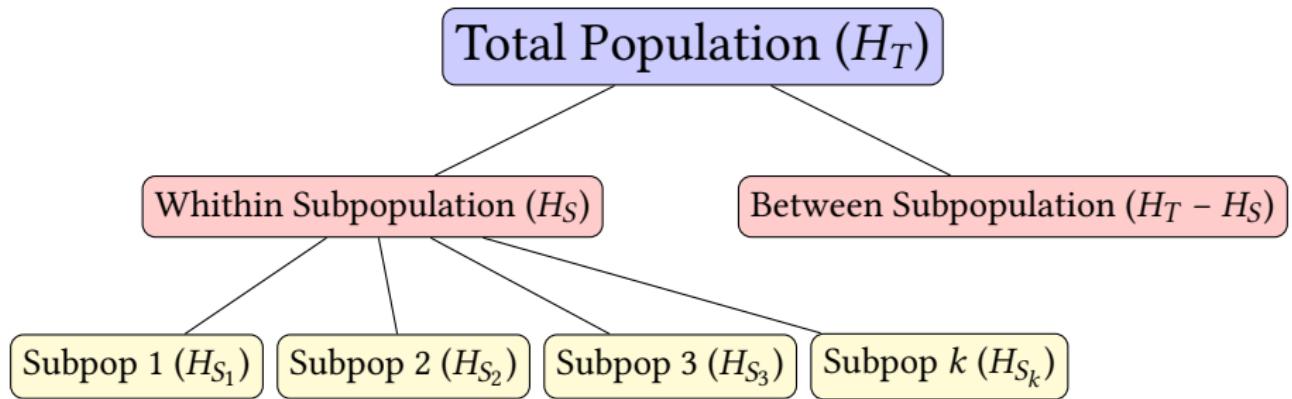
 ANOVA & CR Designs ...

	D.F.	M.S.
Between	$T - 1$	“variance between means”
Within	$T \times (R - 1)$	“mean of within variances”
Total	$T \times R - 1$	

Recapping ...

Parameter		Estimator
Population (by locus)	$He_l(H_{T_l})$	$= 1 - \sum_a \hat{p}_{a_l}^2$
Population (average)	$He(H_T)$	$= \frac{1}{L} \sum_l^L He_l$
Subpopulation i (by locus)	He_{i_l}	$= 1 - \sum_a \hat{p}_{i_a_l}^2$
Subpopulation i (average)	He_i	$= \frac{1}{L} \sum_l^L He_{i_l}$
Within Subpopulation	H_S	$= \frac{1}{I} \sum_i^I He_i$
Between Subpopulation	D_{ST}	$= H_T - H_S$

$$\text{Total} = \text{Between} + \text{Within}$$



≠ Wright Statistics (F) ...

F_{IS} Heterozygosity proportional deviations within subpopulations:

$$F_{IS} = \frac{H_S - Ho}{H_S} [-1; 1]$$

F_{IT} Overall heterozygosity proportional deviation (inbreeding coefficient):

$$F_{IT} = \frac{H_T - Ho}{H_T} [-1, 1]$$

F_{ST} Heterozygosity proportional deviation between subpopulations:

$$F_{ST} = \frac{H_T - H_S}{H_T} [0; 1]$$

Nei, 1987 [4] ...:

1. Obtain H_T :

$$H_T = \frac{1}{L} \sum_l^L He_l$$

2. Obtain H_s (by locus):

$$H_S = \frac{1}{L} \sum_l^L He_{S_l}$$

3. Thus, obtain G_{ST} :

$$G_{ST} = \frac{D_{ST}}{HT} = \frac{H_T - H_S}{H_T} = 1 - \frac{H_S}{H_T}$$

Berg, 1997 [1] ...:

1. Obtain G_{ST} by locus:

$$G_{ST} = \frac{D_{ST}}{H_T} = \frac{H_T - H_S}{H_T} = 1 - \frac{H_S}{H_T}$$

2. Summarize as average:

$$\bar{G}_{ST} = \frac{1}{n_a} \sum_n^{n_a} G_{ST_n}$$

3. That is the same as:

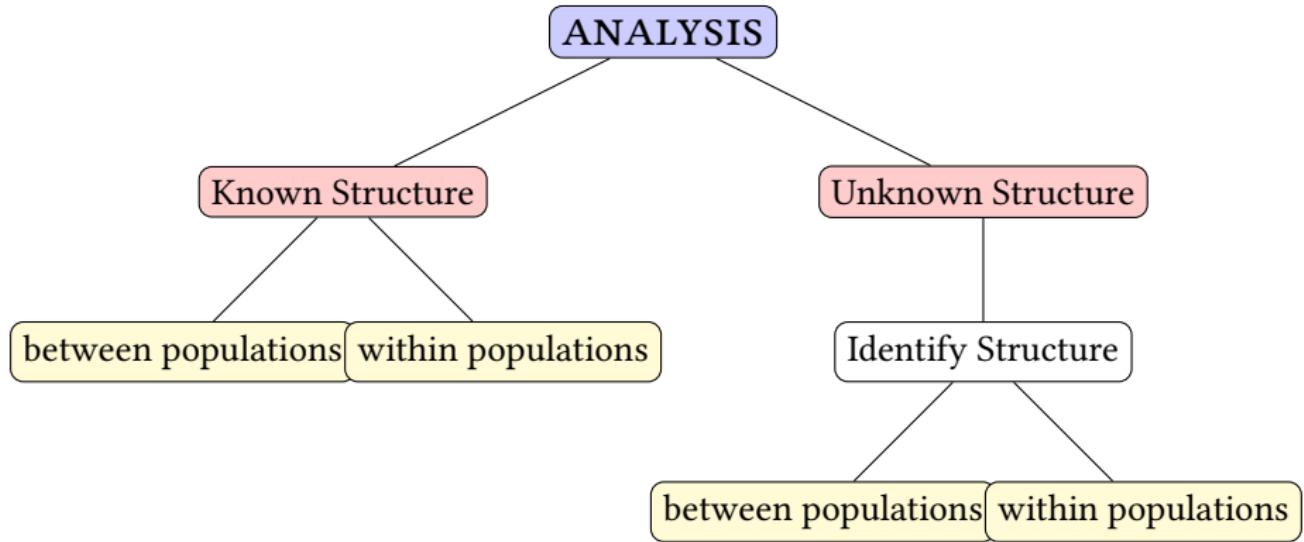
$$\bar{G}_{ST} = 1 - \frac{\sum_n^{n_a} \left(\frac{H_{S_n}}{H_{T_n}} \right)}{n_a}$$

Be aware ... 

- When we have just one (1) allele: $G_{ST} = F_{ST}$;
- G_{ST} generalizes F_{ST} ;
- G_{ST} is the proportion of total diversity that is between subpopulations; and
- Thus, $(1 - G_{ST})$ is the proportion of total diversity within subpopulations.
- The meaning of diversity according to F_{ST} :

F_{ST}	means
[0; 0.05)	small
[0.05; 0.15)	medium
[0.15; 0.25)	high
≥ 0.25	very high

...Intraspecific Diversity (*2nd branch*)



Clusters & Groups ...



OBJECTIVE:

Minimize within variability → Maximize between variability

References can be consulted for deep understanding:

- Fundation book ... [5];
- Fundation paper in genetics (Nei) ... [4]; and
- More modern reference ... [6].

$$\mathbf{Y}_{n \times p} = \begin{bmatrix} y_{1,1} & y_{1,2} & y_{1,3} & \cdots & y_{1,p} \\ y_{2,1} & y_{2,2} & y_{2,3} & \cdots & y_{2,p} \\ y_{3,1} & y_{3,2} & y_{3,3} & \cdots & y_{3,p} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ y_{n,1} & y_{n,2} & y_{n,3} & \cdots & y_{n,p} \end{bmatrix}$$



NOTE:

Everything starts from obtaining the distance matrix between all 2×2 pairs ...

$$\frac{n(n - 1)}{2}$$

$$\mathbf{D} = \begin{bmatrix} 0 & d_{1,2} & d_{1,3} & \cdots & d_{1,j} & \cdots & d_{1,n} \\ 0 & d_{2,3} & \cdots & d_{2,j} & \cdots & d_{2,n} \\ 0 & \cdots & d_{3,j} & \cdots & d_{3,n} \\ \ddots & \vdots & & & \vdots \\ 0 & \cdots & d_{j,n} \\ \ddots & \vdots & & & 0 \end{bmatrix}$$

$d_{i,i} = 0.0$ and D is symmetric $\therefore d_{i,j} = d_{j,i}$

Clustering Methods

- **Geometrical:**
 - Hierarchical;
 - Neighbor Joining;
 - *k-means* (density search); and others
- **MANOVA:**

$$\text{Total} = \text{Between} + \text{Within}$$

- **Statistical:**

Mixture and Bayesian (STRUCTURE)

Hierarchical:

1. All distances;
2. Find the most close individuals (smaller distance); and
3. Iterate over that.
 - UPGMA: merge groups with smaller distance;
 - WARD: merge groups that generate a new one with smaller $S.S.W$; and
 - NJ: merge groups if: (i) smaller distance & (ii) higher distances in comparison to the others.

Bayesian:

The model account for the presence of HW or LD, introduces population structure... find population structure (groups) with the smaller possible disequilibrium [6].

❖ Multidimensional Scaling ...

Two concepts:

1. **Similarity ($s_{[x,y]}$)**: $d_{[x,y]} = \sqrt{2 \times (1 - s_{[x,y]})}$;

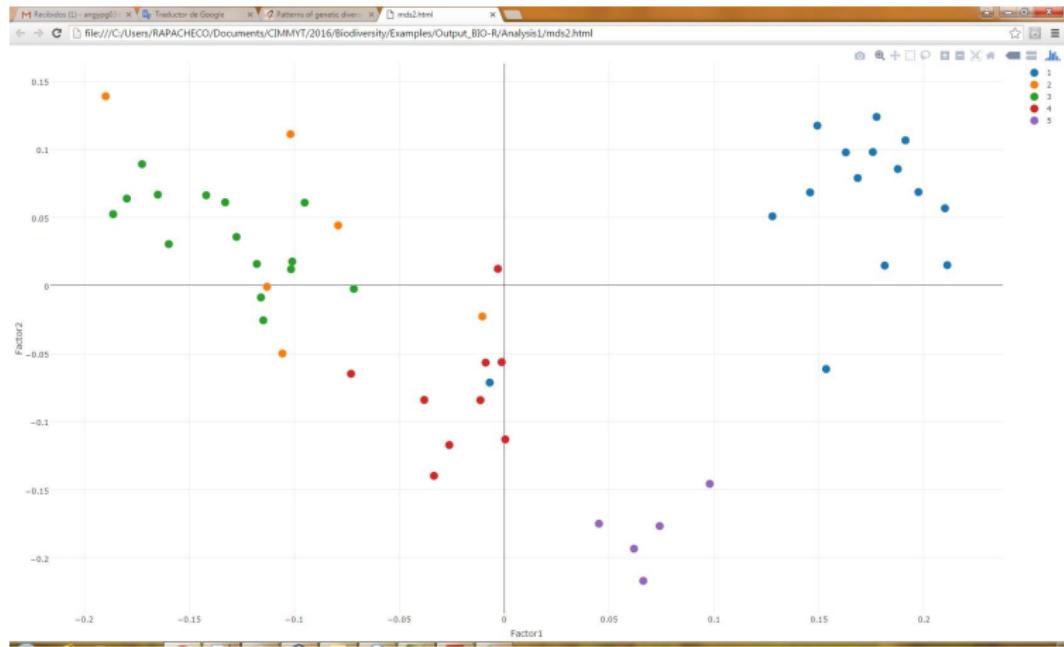
2. **stress (S)**: $S = \sqrt{\frac{\sum_x \sum_y \left(d_{[x,y]} - \mu_{d_{[x,y]}} \right)^2}{\frac{n(n-1)}{2}}}$



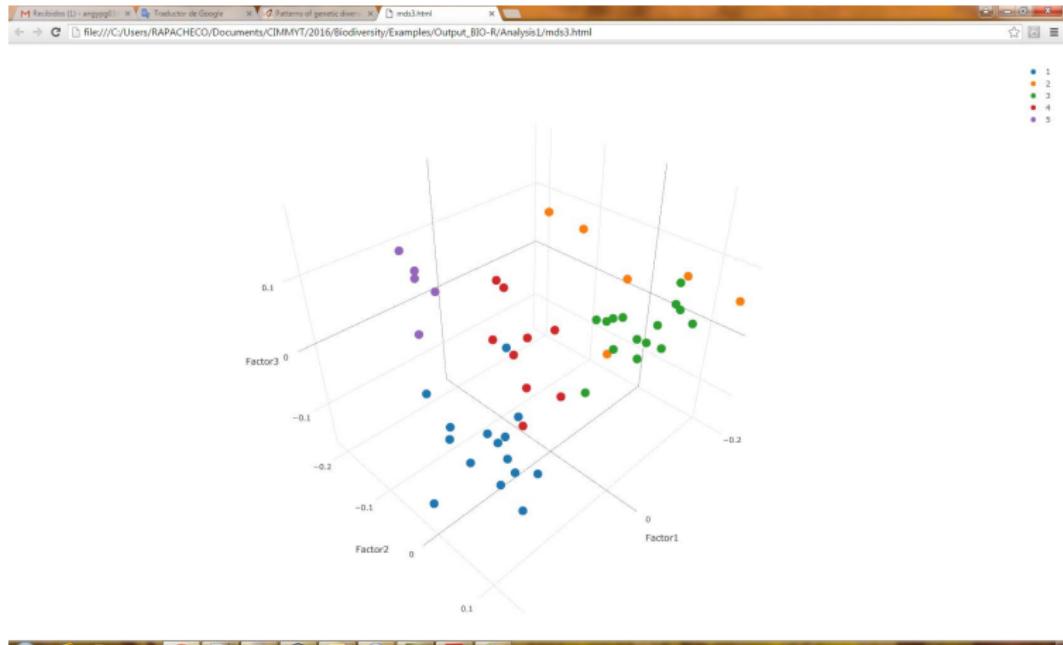
NOTE:

Search for the reduced representation (2 or 3 dimensions) that minimizes the $S.S.B$ in the p dimensional space and with minimum the estimated distance.

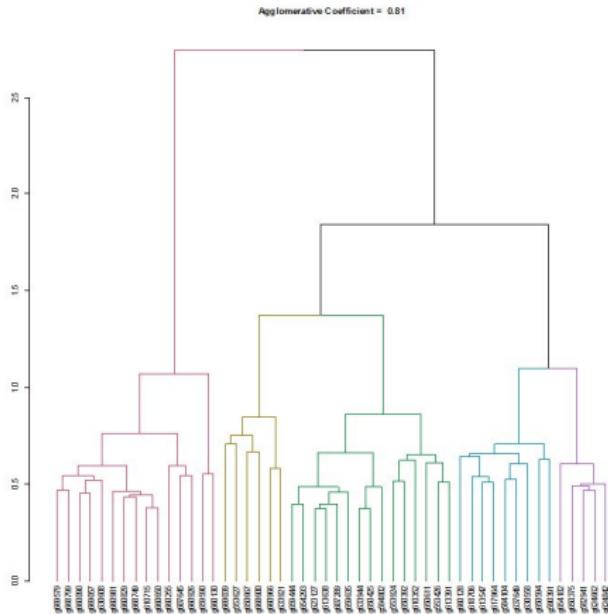
Diversity theory

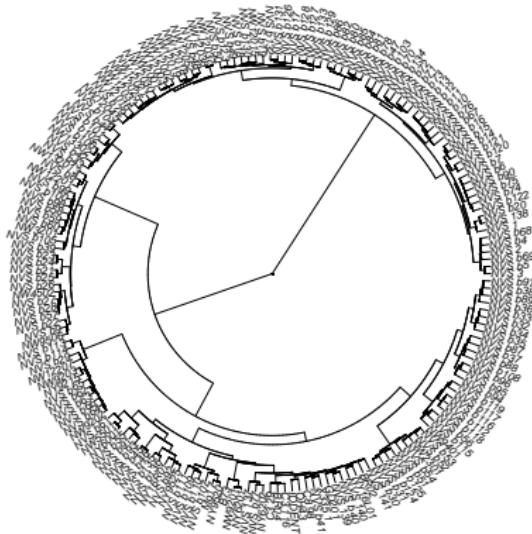


Diversity theory



≠ Dendograms ...





?

BIO-R Tutorial

- Phenotypic data

- *Experimental Design*: ADEL, AUDE & STAD;
- *Individual & Multi-Env*: META (> 1500), AGD (> 1300);
- *Interaction/Stability*: GEA (> 1800); and
- *Spatial Analysis*: SPAT.

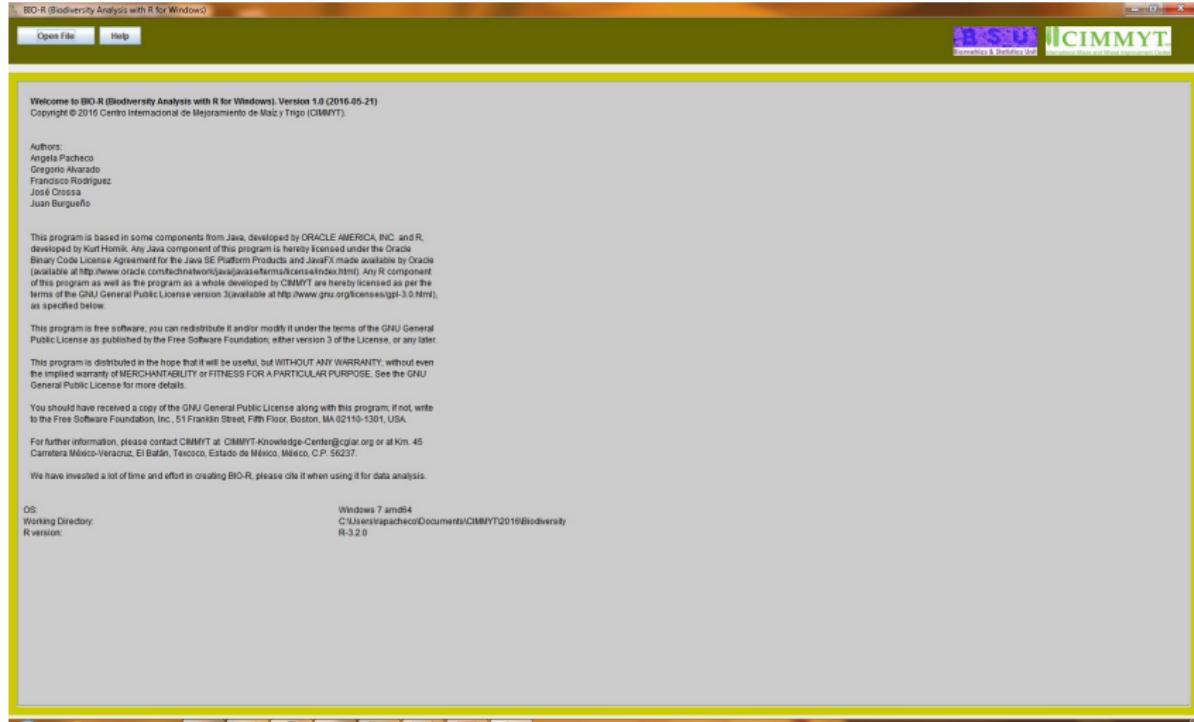
- Genotypic data

- *kinship*: BROWSE & COP; and
- *Diversity*: BIO.

- Fusion data

- *Relationship/Interaction*: GEA;
- *Genome prediction*: BGLR (*R package & application tool); and
- *Selection Index*: SI (> 300), RINDSEL.

- **Decision:** Eval $L \times T$.



?

Downloading and Installation

- BIO-R is already available **go to:** <http://data.cimmyt.org>;
- Java interface/application for  embedding *R* [7] scripts to perform Diversity analysis; and
- heterozygosity, diversity B & W groups, shannon index, number of effective allele, % of polymorphic loci, Rogers & Nei distance, clusters and multidimensional scaling (2 & 3d plots).



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CIMMYT Dataverse Network >

CIMMYT Research Software Dataverse

BIO-R (BIODIVERSITY ANALYSIS WITH R FOR WINDOWS) VERSION 1.0

hdl:11529/10820

Version: 2—Released: Tue Dec 06 09:03:26 CST 2016

POWERED BY THE
 PROJECT
v. 3.0

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Distribution Date	diciembre 06, 2016
Deposit Date	diciembre 06, 2016
Provenance	CIMMYT Research Software Dataverse

② Getting Help & Manual

The Help button will provide you two options:

- **Manual:** *.pdf document describing all options, methods and outputs.

USER'S MANUAL BIO-R (Biodiversity Analysis with R)

- **About:** How to cite BIO-R and any associated license (GNU & Oracle)

② Data Format – *MyData.csv*

<i>mark</i>	<i>g1</i>	<i>g2</i>	<i>g3</i>	<i>g4</i>	...	<i>gX</i>
1	0.67	NA	0.57	NA	...	1
2	NA	1	1	1	...	NA
3	1	1	0.52	0.50	...	0.80
4	1	NA	0.50	1	...	NA
5	1	NA	1	NA	...	1
6	0.67	0	0.71	1	...	0.33
7	1	NA	0	1	...	1
8	1	NA	1	1	...	1
9	NA	1	0.60	0.22	...	0.71
:	:	:	:	:	:	:
<i>N</i>	1	1	1	1	...	1

② Setup ...

1. *Markers* – selects the column that identify the **markers**;
2. *# Clusters* – type the number of groups to split the population;
3. *Output folder* – type the path of the output folder where results will be saved;
 - It will be created inside the BIO-R's Output folder;
 - You can change the name for different sets; and
 - It is necessary to change the name for each analysis.
4. *Genotypes* – selects the columns that identify the **genotypes**;
5. *Distance* – selects the method to calculate **distances**; and
6. *ColorMDSPlot ... [CONT.]*

② ColorMDSPlot

Specify a *.csv file containing additional information for colors in MDS plot

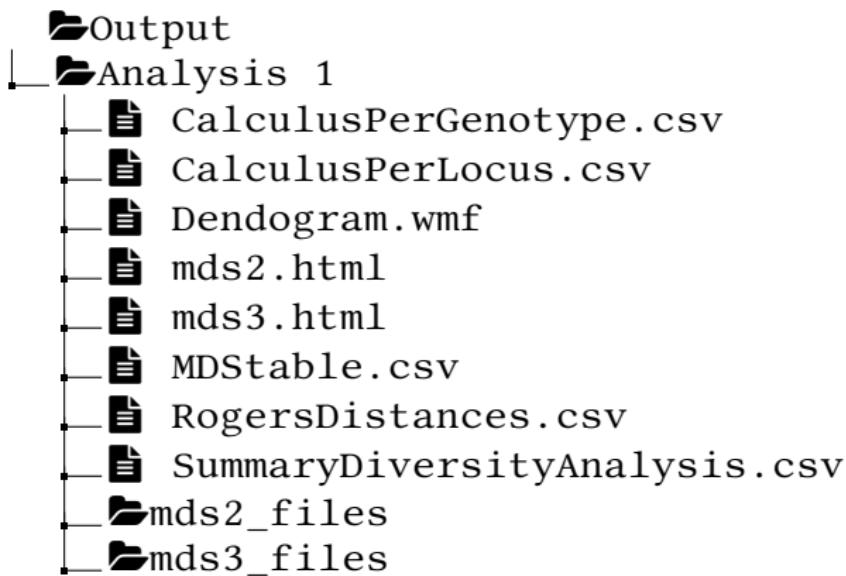
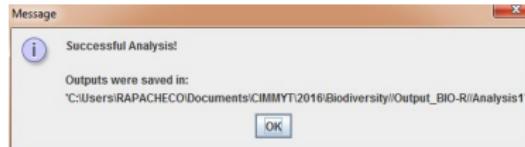
Column 1: the name of the genotypes – should be equal to the input data;

Column 2: the variable to identify the groups of different colours; and

Column 3: any additonal information.

<i>Genotype</i>	<i>NumColor</i>	<i>Something</i>
<i>g669579</i>	<i>11</i>	<i>I</i>
<i>g669039</i>	<i>3</i>	<i>A</i>
<i>g659444</i>	<i>8</i>	<i>F</i>
<i>g660128</i>	<i>11</i>	<i>I</i>
:	:	:
<i>g660829</i>	<i>11</i>	<i>I</i>

② Outputs ...



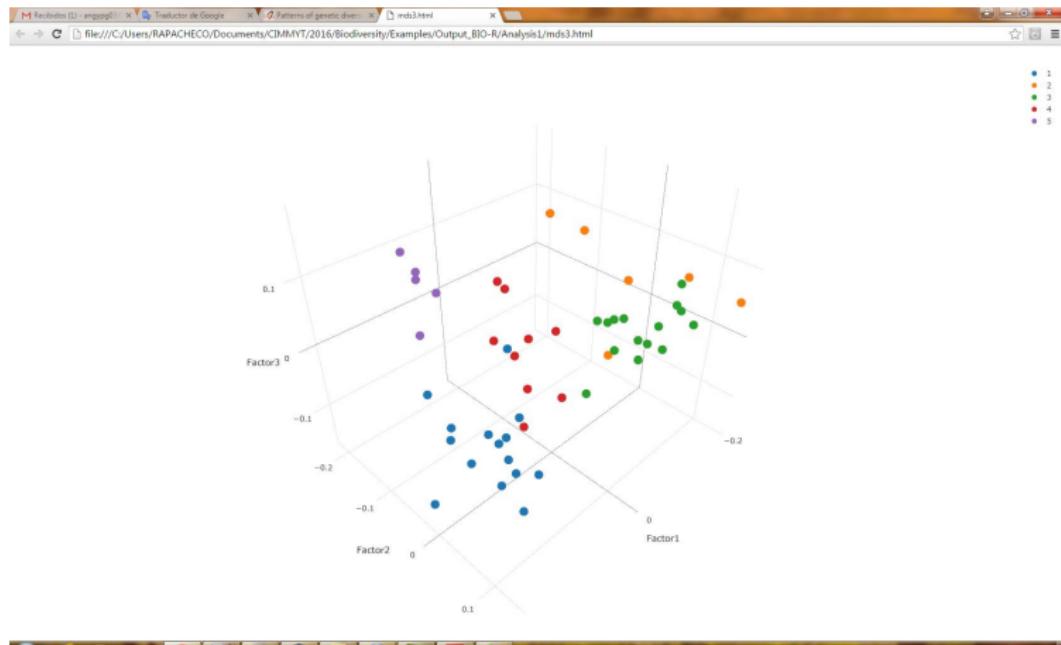
Output : *CalculusPerLocus.csv*

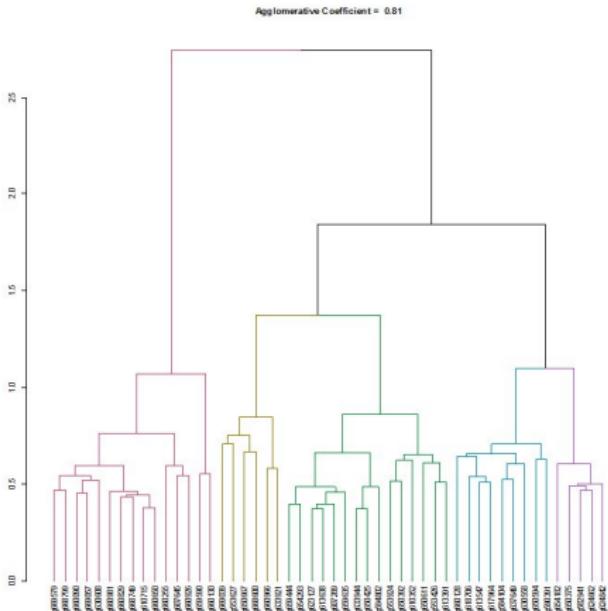
<i>Marker</i>	<i>He</i>	<i>Ho</i>	<i>Ae</i>	<i>Shannon</i>	<i>%NA</i>
1	0.50	0.29	1.99	0.95	0.22
2	0.01	-0.05	1.01	0.02	0.08
3	0.45	0.38	1.82	0.93	0.16
4	0.41	0.42	1.69	0.87	0.24
5	0.03	-0.08	1.03	0.11	0.10
6	0.40	0.43	1.68	0.86	0.20
7	0.50	0.31	2.00	0.99	0.24
8	0.49	0.47	1.94	0.98	0.18
9	0.45	0.47	1.82	0.93	0.14
:	:	:	:	:	:
<i>N</i>	0.08	-0.03	1.09	0.26	0.12

Output : ***CalculusPerGenotype.csv***

Genotype	He	Ho	Ae	Shannon	%NA	clusterGroup
1	0.39	0.06	1.63	0.83	0.11	1
2	0.38	-1.46	1.62	0.82	0.37	2
3	0.40	0.51	1.67	0.85	0.03	3
4	0.39	0.03	1.64	0.83	0.19	4
5	0.37	0.39	1.60	0.81	0.03	3
6	0.41	-3.56	1.69	0.86	0.42	1
7	0.39	0.34	1.65	0.84	0.04	3
8	0.37	-0.28	1.54	0.81	0.24	5
9	0.40	-0.70	1.61	0.82	0.32	1
:	:	:	:	:	:	:
X	0.38	0.33	1.66	0.84	0.04	3

Diversity theory



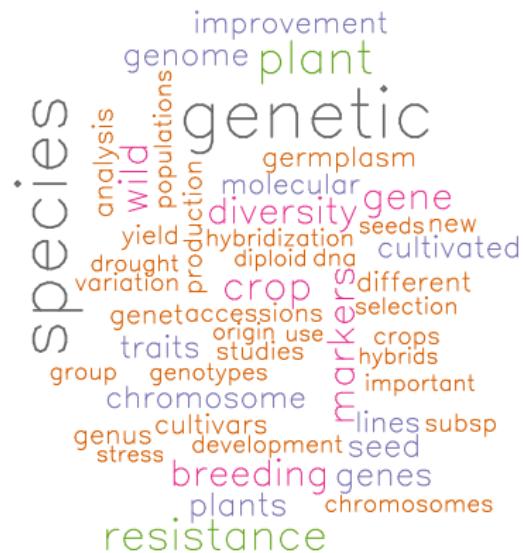


Summary : **SummaryDiversityAnalysis.csv**

- **% of polymorphic loci:** 0.94;
- **Exp. Heterozygosity:** 0.30;
- **Std. Dev. of He :** 0.01;
- **Obs. Heterozygosity:** 0.22;
- **Std. Dev. of Ho :** 0.01;
- **Number of effective alleles:** 1.55;
- **Std. Dev. of Ae :** 0.02;
- **Shannon Index:** 0.63;
- **Std. Dev. Shannon:** 0.02 ...

► Remarks

- Frequency of Alleles & Genotypes;
(Population Genetics) The fundamental concept!
- Distances & Diversity Indices;
(Genetic Diversity) Several ways and flavors.
- Wright Statistics;
(Intraspecific Diversity) Between/Within variability
- BIO-R; and
(Software) it has been built considering everything you may want



❑ Questions/Suggestions?? ❑

For Further Studies:

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- [3] REIF, J. C.; MELCHINGER, A. E.; FRISH, M. Genetical and mathematical properties of similarity and dissimilarity coefficients applied in plant breeding and seed bank management. *Crop Science*, v. 45, p. 1–7, 2005.
- [4] SAITOU, N.; NEI, M. The neighbour-joining method: A new method fo reconstructing phylogenetic trees. *Molecular Biology and Evolution*, v. 4, n. 4, p. 406–425, 1987.
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